

## LO-6

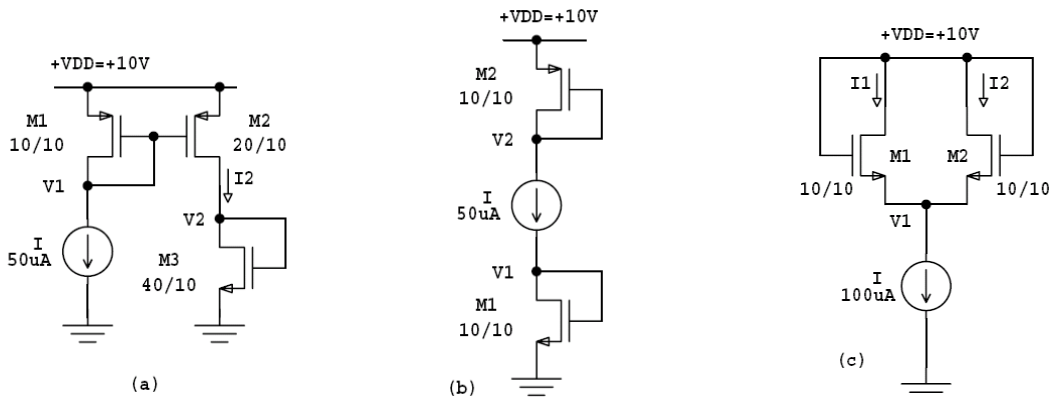
### The Analysis and Design of Currents Mirrors and Active Loads

1. For the CMOS circuits shown in Figs. a,b,c,d, determine the operating modes (CUT-OFF, NONSAT, SAT) for all transistors. Find all labeled DC voltages and currents. Show all your work. For each of the circuits, put your results in a table. All devices have the same parameters;

NMOS transistors:  $\mu_n C_{ox} = 40 \mu A/V^2$ ,  $V_{TN} = 0.7V$

PMOS transistors:  $\mu_p C_{ox} = 20 \mu A/V^2$ ,  $V_{TP} = -0.7V$

For both NMOS and PMOS transistors, channel-length modulation and body effects can be neglected, i.e.,  $\lambda \approx 0$ ,  $\gamma \approx 0$ . The DC bias voltage sources VDD, VSS and current sources are assumed ideal.



2. In the CMOS circuit shown below,

NMOS transistors:

$\mu_n C_{ox} = 50 \mu A/V^2$ ,  $V_{TN} = 1V$ ,  $\lambda_n = 0.02 1/V$ ,  $\gamma_n = 0$ .

PMOS transistors:

$\mu_p C_{ox} = 16 \mu A/V^2$ ,  $V_{TP} = -1V$ ,  $\lambda_p = 0.02 1/V$ ,  $\gamma_p = 0$ .

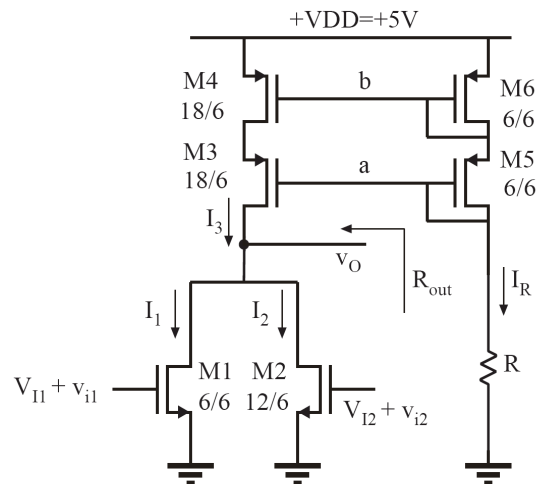
The supply voltage is  $V_{DD} = 5V$ . The two input voltages have DC bias components  $V_{I1}$ ,  $V_{I2}$ , and the small signal components  $v_{i1}$ ,  $v_{i2}$ . The device sizes  $W/L$  in  $\mu m$  are shown in the Figure. (State the approximations you made in solving the problem.)

- a) For  $V_{I1} = V_{I2} = 1.4V$ , resistance  $R$  selected so that all devices operate in the active mode. Find the DC bias currents  $I_1$ ,  $I_2$ ,  $I_3$ ,  $I_R$  and the DC bias voltages  $V_a$ ,  $V_b$ . Find  $R$ .

- b) For  $V_{I1} = V_{I2} = 1.4V$ , and  $R$  found in (a), find the range of the output voltages  $V_{Omin} < V_O < V_{Omax}$ , such that all devices operate in the active mode.

In parts (c) and (d) of the problem, you can assume that the circuit operates at the point found in (a), and that  $V_O$  is such that all devices are active.

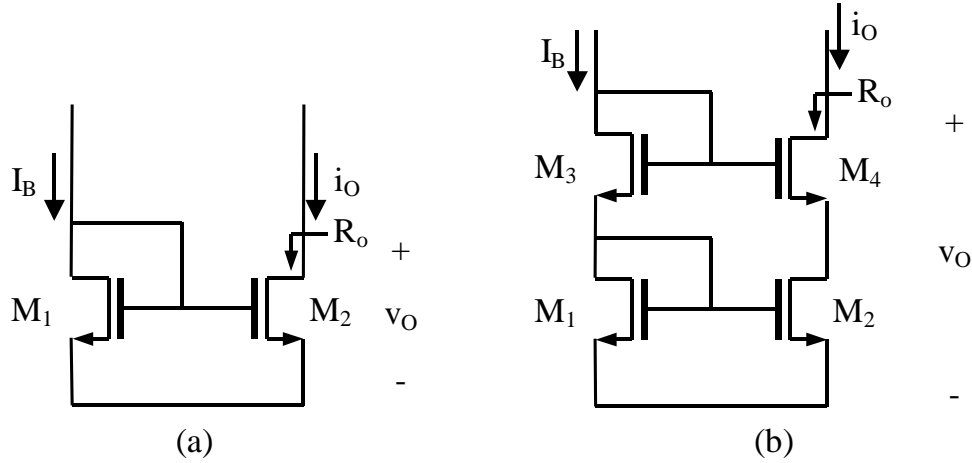
- c) Find the parameters  $g_{m1}$ ,  $r_{ds1}$ ,  $g_{m2}$ ,  $r_{ds2}$  in the small-signal models of the devices M1 and M2.  
d) Find the small-signal output  $v_o$  as a function of the small-signal inputs  $v_{i1}$ ,  $v_{i2}$ . Find the output resistance  $R_{out}$ .  
e) If  $V_{I1} = 5V$  and  $V_{I2} = 0V$ , and  $R$  is as found in (a), determine operating modes of all devices. Justify your answers.



3. Consider the following current mirrors. These current mirrors are to be used as current sources.

For each current mirror

- Express  $i_o = I_{OQ}$  in terms of the biasing current  $I_B$  where  $I_B > 0$ .
- Determine the limits on  $I_{OQ}$  and  $V_{OQ}$ .
- What is the small signal equivalent resistance  $R_o$  seen from the output port.
- Compare the results.



4. In the Wilson current mirror shown, assume the transistors' parameters are

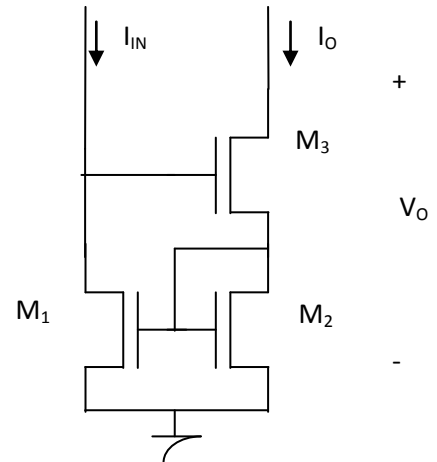
$$V_T = 0.75 \text{ V}, K_n = 48 \mu\text{A}/\text{V}^2,$$

The aspect ratios are

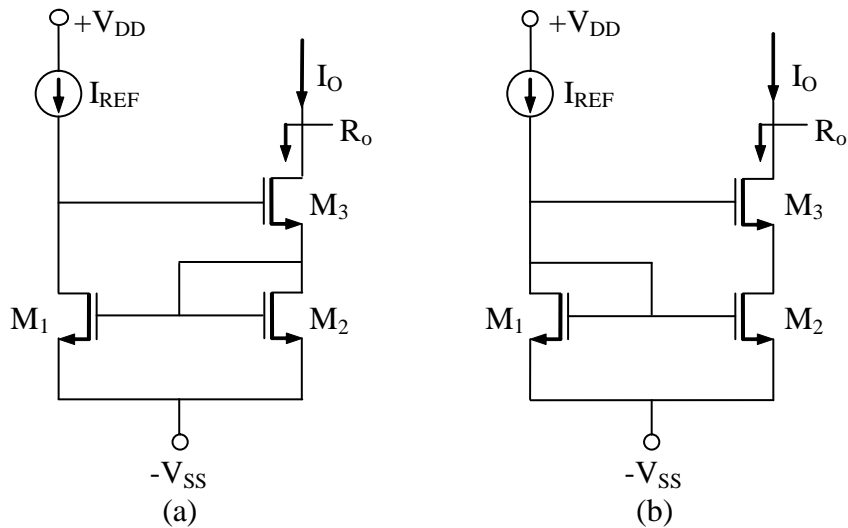
$$W_1/L_1 = W_2/L_2 = W_3/L_3 = 5$$

for  $M_1$ ,  $M_2$ , and  $M_3$  respectively.

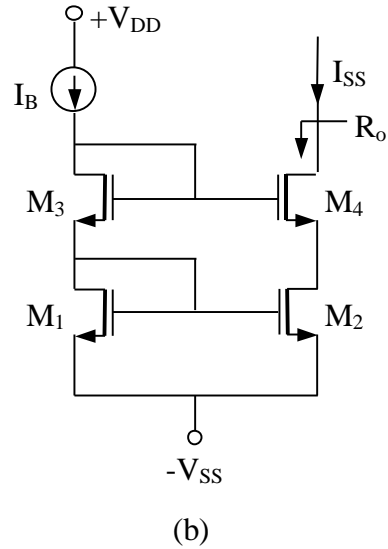
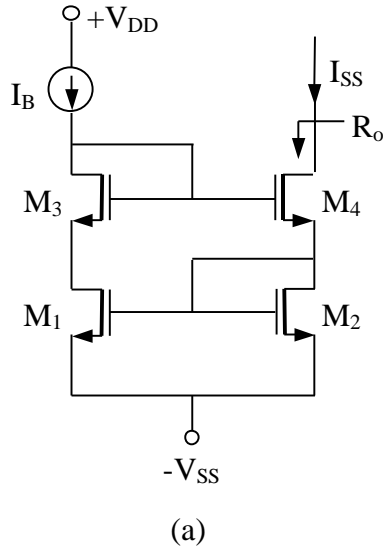
Determine and plot the family of output current  $I_o$  characteristics as a function of  $V_o$ , where  $I_{IN}$  is the parameter to be varied to obtain the family of curves.



5. For the current sources given below, assume the transistors  $M_1$ ,  $M_2$ ,  $M_3$  and  $M_4$  are identical, i.e., they have the same process parameters and the same aspect ratios.



- a) Express the output current  $I_0$  in terms of  $I_{REF}$  and the circuit and transistor parameters.
  - b) Assuming that  $g_{m1} = g_{m2} = g_{m3} = g_m$  and  $r_{ds1} = r_{ds2} = r_{ds3} = r_o$ , determine the output resistances  $R_o$ 's.
  - c) Compare the circuits given in (a) and (b).
6. For the current sources given below, compare the small signal output resistances as defined below. Assume  $M_1, M_2, M_3$  and  $M_4$  are identical, i.e., they have the same process parameters and the same aspect ratios.



For the circuits given in (a) and (b), assuming that

$$g_{m1} = g_{m2} = g_{m3} = g_{m4} = g_m$$

$$r_{ds1} = r_{ds2} = r_{ds3} = r_{ds4} = r_o$$

- a) Express the output current  $I_{SS}$  in terms of  $I_B$  and the circuit and transistor parameters
- b) Determine the output resistances  $R_o$ 's, and compare them.